

# CDSIMEQ: A program to implement two-stage probit least squares

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**Abstract.** The `cdsimeq` command implements the two-stage estimation method described in Maddala (1983) for simultaneous equations models in which one of the endogenous variables is continuous and the other endogenous variable is dichotomous. The `cdsimeq` command implements all the necessary procedures for obtaining consistent estimates for the coefficients, as well as their corrected standard errors.

**Keywords:** st0000, simultaneous equations, Maddala, continuous endogenous, dichotomous endogenous, 2SPLS<sup>1</sup>, 2SLS, instruments, standard errors

## 1 Introduction

The problem of simultaneity (or reciprocal causation) and methods of estimating such relationships has been widely discussed in the statistical literature (for general introductions, see Gujarati (1995) and Pindyck and Rubinfeld (1991); for more advanced expositions, see Davidson and MacKinnon (1993), Greene (2000), and Judge et al. (1985)). At issue is the problem that standard estimation methods in the presence of simultaneity will result in biased and inconsistent estimates. This bias can be corrected by choosing one of two popular methods: indirect least squares (ILS) or two-stage least squares (2SLS). The main focus of the literature, however, has been on situations where the endogenous variables are continuous across equations.

In social science research, however, many phenomena of interest can take on only two values or can only be observed as dichotomies. For example, a person either voted or did not vote. This is an example of a phenomenon that naturally has only two possible values. In other cases, such as involvement in militarized interstate disputes, one can argue that the propensity to engage in such disputes is a continuous underlying process, but this propensity can only be observed as a dichotomy; i.e., we can only observe whether a state is/has engaged in a militarized dispute or not. In a single-equation setting, this type of model is easy to fit, and all statistical packages have built-in procedures for estimation; see [R] `probit`, [R] `logit`, and [R] `logistic`.

What if, however, a continuous and a dichotomous variable are hypothesized to simultaneously determine each other? For example, Keshk et al. (1992) are interested

<sup>1</sup>To the best of my knowledge, the term 2SPLS was given to the procedure by Alvarez and Glasgow (2000). Other terms for this procedure include generalized two-stage probit (Amemiya 1978); two-step probit estimator (Guilkey et al. 1992). I prefer 2SPLS because it provides a more complete description of steps and estimations used.

in whether a simultaneous relationship between trade and militarized interstate disputes (MIDs) exists. Trade is a continuous variable whereas MIDs is a dichotomous variable or only observable as a dichotomous variable. In such situations, the options for estimating such relationships using current statistical software packages become extremely limited. This limitation is not due to a lack of statistical literature on how to fit such models, but to the lack of procedures to fit such models in available statistical software packages.<sup>2</sup>

Heckman (1978), Amemiya (1978), and Maddala (1983) all discuss appropriate estimation procedures for such models. Like their continuous counterparts, estimation can proceed through indirect methods (i.e., recovering the structural parameters from reduced form estimates) or through two stage procedures (i.e., creating instruments for the endogenous variables and then substituting them for their endogenous counterparts in the structural equations). In spite of this literature, I am not aware of any statistical package that includes procedures to fit such models. This is puzzling in the age of programmable statistical software programs such as Stata. `cdsimeq` is hopefully a first step in filling this void.

## 2 Background

In order to fully comprehend the usefulness and applicability of the `cdsimeq` command, it is essential to understand the nature of the problem that it is trying to estimate. Equations (1) and (2) present a generic two-equation model,<sup>3</sup>

$$y_1^* = \gamma_1 y_2^* + \beta_1' \mathbf{X}_1 + \varepsilon_1 \quad (1)$$

$$y_2^* = \gamma_2 y_1^* + \beta_2' \mathbf{X}_2 + \varepsilon_2 \quad (2)$$

The proper estimation strategy to be used depends on how  $y_1^*$  and  $y_2^*$  are observed, as well as whether we are dealing with recursive or nonrecursive models. First, if  $y_1 = y_1^*$  and  $y_2 = y_2^*$ ,<sup>4</sup> i.e., both variables are observed, and neither  $\gamma_1$  nor  $\gamma_2$  equal zero, then we have the typical simultaneous equations models discussed in the statistical literature. Methods for fitting such models can be found in the previously cited literature. Stata's `reg3` can fit such models; see [R] `reg3`. If theory or prior expectation leads us to believe that  $\gamma_1 = 0$  or  $\gamma_2 = 0$ , but not both, and the error terms are not contemporaneously correlated, then we have a recursive model and each equation can be estimated separately by OLS.<sup>5</sup>

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<sup>2</sup>To the best of my knowledge, no statistical software packages have procedures for fitting this type of model. One Stata program, `probitiv`, written by Jonah Gelbach fits such models; however, it does not correct the standard errors.

<sup>3</sup>The following discussion borrows heavily from Maddala (1983, 242–7).

<sup>4</sup>This corresponds to Maddala's (1983, 243) model 1.

<sup>5</sup>If the error terms are contemporaneously correlated, then estimation can proceed by using seemingly unrelated regressions or other methods; for examples and full discussion, see Greene (2000).

If  $y_1^*$  and  $y_2^*$  are observed as follows<sup>6</sup>

$$\begin{aligned} y_1 &= y_1^* \\ y_2 &= 1 \text{ if } y_2^* > 0 \\ y_2 &= 0 \text{ otherwise} \end{aligned}$$

and neither  $\gamma_1$  nor  $\gamma_2$  equal zero, then we have a model for which `cdsimeq` is written. How to fit such a model is discussed in the next section. If, however, theory or prior expectation leads us to believe that  $\gamma_2 = 0$ , then we have two interesting situations.

First, if it is hypothesized that  $y_1^*$  is only observed given some selection criterion defined by another variable, in this case  $y_2^*$ , then we have an example of a sample selection model. While the details of such models are beyond the scope of this paper, the interested readers are directed to Barnow et al. (1981), Breen (1996), and Maddala (1983) for discussion of such models and methods for their estimation. Stata's `treatreg` can perform all the necessary estimations (two-stage and maximum likelihood) for such models; see [R] `treatreg`. On the other hand, if  $y_1^*$  is not determined by any selection criterion,  $\gamma_1 = 0$  or  $\gamma_2 = 0$ , but not both, and the error terms are not contemporaneously correlated, then we have a recursive model with a continuous and dichotomous variable and methods for fitting such models are discussed in Maddala and Lee (1976).

A final model of some relevance to our discussion is the following:<sup>7</sup>

$$\begin{aligned} y_1 &= y_1^* \\ y_2 &= y_2^* \text{ if } y_2^* > 0 \\ y_2 &= 0 \text{ otherwise} \end{aligned}$$

If  $\gamma_1$  and  $\gamma_2$  are not equal to 0, then we have what Amemiya (1979) calls a simultaneous equation tobit model. Estimation of such models is fully discussed in Amemiya (1979) and Maddala (1983). Readers interested in fitting such a model can cannibalize `cdsimeq` to do so, since the estimation procedures for both models are very similar.<sup>8</sup> While there are several other model possibilities, their discussion is beyond the scope of this paper and interested readers are directed to Maddala (1983).

### 3 Methods and formulas

`cdsimeq` is written to fit a simultaneous equation model in which one of the variables is continuous and the other is dichotomous and as was shown above, this is but one possible model in a class of such models. Adapting current methods for estimating simultaneous equations to a model in which one of the endogenous variables is continuous and the other is dichotomous is straightforward. The only difference is in the appropriate calculation of the standard errors. The discussion that follows will present

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<sup>6</sup>This corresponds to Maddala's (1983, 244–5) model 3.

<sup>7</sup>This corresponds to Maddala's (1983, 243–4) model 2.

<sup>8</sup>Interested readers should consult Maddala (1983, 243–4).

the estimation method as it pertains to programming and not to statistical derivation. Readers interested in the statistical derivation aspect are directed to Heckman (1978), Amemiya (1978), and Maddala (1983).

We begin with our simultaneous equations model:

$$y_1 = \gamma_1 y_2^* + \beta_1' \mathbf{X}_1 + \varepsilon_1 \quad (3)$$

$$y_2^* = \gamma_2 y_1 + \beta_2' \mathbf{X}_2 + \varepsilon_2 \quad (4)$$

where

$y_1$  is a continuous endogenous variable,

$y_2^*$  is a dichotomous endogenous variable, which is observed as a 1 if  $y_2^* > 0$ , and 0 otherwise,

$\mathbf{X}_1$  and  $\mathbf{X}_2$  are matrices of exogenous variables in (3) and (4),

$\beta_1'$  and  $\beta_2'$  are vectors of parameters in (3) and (4),

$\gamma_1$  and  $\gamma_2$  are the parameters of the endogenous variables in (3) and (4),

$\varepsilon_1$  and  $\varepsilon_2$  are the error terms of (3) and (4).

Because  $y_2^*$  is not observed, the structural equations (3) and (4) are rewritten as

$$y_1 = \gamma_1 \sigma_2 y_2^{**} + \beta_1' \mathbf{X}_1 + \varepsilon_1 \quad (5)$$

$$y_2^{**} = \frac{\gamma_2}{\sigma_2} y_1 + \frac{\beta_2'}{\sigma_2} \mathbf{X}_2 + \frac{\varepsilon_2}{\sigma_2} \quad (6)$$

Now estimation follows the typical two-stage estimation process. In the first stage, the following two models are fitted using all of the exogenous variables (i.e., the exogenous variables in both (5) and (6)),

$$y_1 = \boldsymbol{\Pi}_1' \mathbf{X} + v_1 \quad (7)$$

$$y_2^{**} = \boldsymbol{\Pi}_2' \mathbf{X} + v_2 \quad (8)$$

where

$\mathbf{X}$  is a matrix of all the exogenous variables in (5) and (6),

$\boldsymbol{\Pi}_1$  and  $\boldsymbol{\Pi}_2$  are vectors of parameters to be estimated,

$v_1$  and  $v_2$  are error terms.

Equation (7) is estimated via OLS and (8) via probit. From these reduced-form estimates, the predicted values from each model are obtained for use in the second stage.

$$\hat{y}_1 = \hat{\boldsymbol{\Pi}}_1 \mathbf{X} \quad (9)$$

$$\hat{y}_2^{**} = \hat{\boldsymbol{\Pi}}_2 \mathbf{X} \quad (10)$$

In the second stage, the original endogenous variables in (5) and (6) are replaced by their respective fitted values in (9) and (10). Thus, in the second stage, the following two models are fitted:

$$y_1 = \gamma_1 \hat{y}_2^{**} + \beta_1 \mathbf{X}_1 + \varepsilon_1 \quad (11)$$

$$y_2^{**} = \gamma_2 \hat{y}_1 + \beta_2 \mathbf{X}_2 + \varepsilon_2 \quad (12)$$

Again, (11) is estimated via OLS and (12) is estimated via probit.

The final step in the procedure is the correction of the standard errors. This is necessary because, as can be seen from (11) and (12), the outputted standard errors for each model in the second stage will be based on  $\hat{y}_2^{**}$  and  $\hat{y}_1$  and not on the appropriate  $y_2^{**}$  and  $y_1$ . Thus, the estimated standard errors in (11) and (12) will be incorrect. The correction that needs to be implemented on the variance–covariance matrices  $\alpha_1$  and  $\alpha_2$ , which are the variance–covariance matrices of (11) and (12), respectively, is as follows: First define the following:<sup>9</sup>

$$\begin{aligned} \alpha'_1 &= (\gamma_1 \sigma_2, \beta'_1) \\ \alpha'_2 &= \left( \frac{\gamma_2}{\sigma_2}, \frac{\beta'_2}{\sigma_2} \right) \\ c &= \sigma_1^2 - 2\gamma_1 \sigma_{12} \\ d &= \left( \frac{\gamma_2}{\sigma_2} \right) \sigma_1^2 - 2 \left( \frac{\gamma_2}{\sigma_2} \right) \left( \frac{\sigma_{12}}{\sigma_2} \right) \\ H &= (\Pi_2, J_1) \end{aligned} \quad (13)$$

$$G = (\Pi_1, J_2) \quad (14)$$

$$V_0 = \text{Var}(\hat{\Pi}_2) \quad (15)$$

With these definitions at hand, and noting that in probit models  $\sigma_2$  is normalized to 1, the corrected variances of  $\alpha_1$  and  $\alpha_2$  can be obtained as follows:

$$V(\widehat{\alpha}_1) = c(H' X' X H)^{-1} + (\gamma_1 \sigma_2)^2 (H' X' X H)^{-1} H' X' V_0 X' X H (H' X' X H)^{-1} \quad (16)$$

$$V(\widehat{\alpha}_2) = (G' V_0^{-1} G)^{-1} + d(G' V_0^{-1} G)^{-1} G' V_0^{-1} (X' X)^{-1} V_0^{-1} G (G' V_0^{-1} G)^{-1} \quad (17)$$

Everything defined above is easily obtainable from built-in Stata procedures, while others can be obtained by programming Stata. The following are easily obtained via built-in Stata procedures:

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<sup>9</sup>What follows is from Maddala (1983, 244–5).

1. The predicted values in (9) and (10) are easily obtained in Stata after running the appropriate statistical procedures.
2.  $\sigma_1^2$  is the variance of the residuals from (7) and is easily available in Stata after estimating (7).
3.  $\Pi_1$  in (13) and  $\Pi_2$  in (14) are the coefficient matrices from (9) and (10) and are available from within Stata, after each estimation.
4.  $V_0$  in (15) is easily obtained from within Stata, after running the probit estimation in (10).

All other values are obtainable through a little programming. For example,

1.  $\mathbf{J}_1$  and  $\mathbf{J}_2$  are matrices with ones and zeros such that  $\mathbf{X}\mathbf{J}_1 = \mathbf{X}_1$  and  $\mathbf{X}\mathbf{J}_2 = \mathbf{X}_2$ . To create these matrices, a loop procedure is used. Thus, in the creation of  $\mathbf{J}_1$ , the loop checks the location of exogenous variables in  $\mathbf{X}$  against the location of exogenous variables in  $\mathbf{X}_1$ . The loop then places a one in the row of  $\mathbf{J}_1$  for the column location of the exogenous variable, say  $x_1$ , in  $\mathbf{X}$  and simultaneously a one in the column of  $\mathbf{J}_1$  for the column location of  $x_1$  in  $\mathbf{X}_1$ . A similar loop is used for the creation of the  $\mathbf{J}_2$  matrix.
2. Programming is also needed to obtain  $\sigma_{12}$ . It is obtained using the formula  $1/N\{\sum(d_t\hat{v}_1)/\hat{f}\}$  (Amemiya 1978, 1200), where
  - a.  $N$  is the number of observations.
  - b.  $d_t$  is the dichotomous endogenous variable.
  - c.  $\hat{v}_1$  is the residuals from (7).
  - d.  $\hat{f}$  is (10) evaluated using the standard normal density.
3. Finally, the corrections outlined in (16) and (17) are easily obtained using matrix routines within Stata, and the resulting output is easily generated using Stata's estimates post and repost features, see [P] **estimates**.

## 4 Syntax

```
cdsimeq (continuous_endogenous_depvar continuous_model_exogenous_indvar(s))
         (dichotomous_endogenous_depvar dichotomous_model_exogenous_indvar(s))
         [if exp] [in range] [, nofirst nosecond asis instpre estimates hold]
```

### 4.1 Options

`nofirst` specifies that the displayed output from the *first stage* estimations be suppressed.

`nosecond` specifies that the displayed output from the second stage estimations be suppressed.

`asis` is Stata's `asis` option; see [R] **probit**.

`instpre` specifies that the created instruments in the first stage are not to be discarded after the program terminates. Note that if this option is specified and the program is rerun, an error will be issued saying that the variables already exist. Therefore, these variables have to be dropped or renamed before `cdsimeq` can be rerun.

`estimates_hold` retains the estimation results from the OLS estimation, with corrected standard errors, in a variable called `model_1` and estimation results from the probit estimation, with corrected standard errors, in a variable called `model_2`.<sup>10</sup> Note that if this option is specified the above variables must be dropped before `cdsimeq` command is rerun again with the `estimates_hold` option.

## 4.2 Stata output

Here is a stylized example for `cdsimeq`:

```
. cdsimeq (continuous exog3 exog2 exog1 exog4) ( dichotomous exog1 exog2 exog5
> exog6 exog7)

      NOW THE FIRST STAGE REGRESSIONS

      Source |   SS      df      MS
      Model | 617.390728    7  88.1986754
      Residual | 417.608638  992  .420976449
      Total | 1034.99937  999  1.0360354
      Number of obs = 1000
      F( 7, 992) = 209.51
      Prob > F = 0.0000
      R-squared = 0.5965
      Adj R-squared = 0.5937
      Root MSE = .64883

      continuous |      Coef.      Std. Err.          t      P>|t|
      exog3 | .1584685  .0218622       7.25      0.000  .1155671  .2013699
      exog2 | -.009669  .0216656      -0.45      0.655  -.0521846  .0328466
      exog1 | .1599552  .0212605       7.52      0.000  .1182345  .2016759
      exog4 | .3165751  .0224563      14.10      0.000  .2725079  .3606424
      exog5 | .4972074  .021356       23.28      0.000  .4552993  .5391156
      exog6 | -.0780172  .0217546      -3.59      0.000  -.1207076  -.0353268
      exog7 | .1611768  .022103       7.29      0.000  .1178028  .2045508
      _cons | .0107516  .0206197       0.52      0.602  -.0297117  .051215

Iteration 0: log likelihood = -692.49904
Iteration 1: log likelihood = -424.29883
Iteration 2: log likelihood = -382.05354
Iteration 3: log likelihood = -377.16723
Iteration 4: log likelihood = -377.07132
Iteration 5: log likelihood = -377.07127
```

(Continued on next page)

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<sup>10</sup>When this option is specified the created instruments are also preserved.

Probit estimates  
Number of obs = 1000  
LR chi2(7) = 630.86  
Prob > chi2 = 0.0000  
Pseudo R2 = 0.4555  
Log likelihood = -377.07127

dichotomous	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
exog3	.2134477	.0562479	3.79	0.000	.1032039 .3236916
exog2	.2113067	.0537592	3.93	0.000	.1059406 .3166728
exog1	.4559128	.060367	7.55	0.000	.3375958 .5742299
exog4	.3903133	.0620052	6.29	0.000	.2687852 .5118413
exog5	.7595488	.0646746	11.74	0.000	.6327889 .8863088
exog6	.8546139	.0689585	12.39	0.000	.7194577 .98977
exog7	-.1669142	.0566927	-2.94	0.003	-.2780298 -.0557986
_cons	.0835167	.0528104	1.58	0.114	-.0199899 .1870232

## NOW THE SECOND STAGE REGRESSIONS WITH INSTRUMENTS

Source	SS	df	MS	Number of obs = 1000
Model	429.827896	5	85.9655791	F( 5, 994) = 141.20
Residual	605.17147	994	.608824416	Prob > F = 0.0000
Total	1034.99937	999	1.0360354	R-squared = 0.4153
				Adj R-squared = 0.4124
				Root MSE = .78027

  

continuous	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
I_dichotom-s	.2575918	.0214505	12.01	0.000	.2154983 .2996854
exog3	.0425202	.026735	1.59	0.112	-.0099435 .0949838
exog2	.0118544	.0267226	0.44	0.657	-.0405848 .0642937
exog1	.0077736	.0282168	0.28	0.783	-.0475978 .063145
exog4	.3186363	.0283114	11.25	0.000	.2630793 .3741933
_cons	.0121851	.0248091	0.49	0.623	-.0364991 .0608692

Iteration 0: log likelihood = -692.49904  
Iteration 1: log likelihood = -424.31527  
Iteration 2: log likelihood = -382.0779  
Iteration 3: log likelihood = -377.20169  
Iteration 4: log likelihood = -377.10665  
Iteration 5: log likelihood = -377.10661

Probit estimates  
Number of obs = 1000  
LR chi2(6) = 630.78  
Prob > chi2 = 0.0000  
Pseudo R2 = 0.4554  
Log likelihood = -377.10661

dichotomous	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
I_continuous	1.262866	.1604171	7.87	0.000	.9484539 1.577277
exog1	.2509257	.0649992	3.86	0.000	.1235297 .3783218
exog2	.2260372	.0529623	4.27	0.000	.1222331 .3298413
exog5	.1291197	.0958474	1.35	0.178	-.0587377 .3169771
exog6	.9560943	.0721625	13.25	0.000	.8146584 1.09753
exog7	-.3712822	.0674939	-5.50	0.000	-.5035678 -.2389966
_cons	.0707977	.0528105	1.34	0.180	-.0327091 .1743044

## NOW THE SECOND STAGE REGRESSIONS WITH CORRECTED STANDARD ERRORS

continuous	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
I_dichotom-s	.2575918	.1043332	2.47	0.014	.0528532 .4623305
exog3	.0425202	.1291476	0.33	0.742	-.210913 .2959533
exog2	.0118544	.1290542	0.09	0.927	-.2413956 .2651044
exog1	.0077736	.1363699	0.06	0.955	-.2598323 .2753795
exog4	.3186363	.1367953	2.33	0.020	.0501956 .5870777
_cons	.0121851	.1198708	0.10	0.919	-.2230438 .2474139

  

dichotomous	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
I_continuous	1.262866	.7397385	1.71	0.088	-.1869952 2.712726
exog1	.2509257	.3130259	0.80	0.423	-.3625938 .8644452
exog2	.2260372	.2737467	0.83	0.409	-.3104964 .7625708
exog5	.1291197	.4827168	0.27	0.789	-.8169878 1.075227
exog6	.9560943	.2825678	3.38	0.001	.4022716 1.509917
exog7	-.3712822	.3265683	-1.14	0.256	-1.011344 .2687799
_cons	.0707977	.2666057	0.27	0.791	-.4517399 .5933353

### 4.3 Saved results

`cdsimeq` provides certain saved results depending on whether the option `estimates_hold` was specified. Without the `estimates_hold` option, the following saved results are provided:

## Scalars

e(sigma_11)	$\sigma_{11}$	e(sigma_12)	$\sigma_{12}$
e(gamma_2)	$\gamma_2$	e(gamma_2_sq)	$\gamma_2^2$
e(MA_c)	$\sigma_1^2 - 2\gamma_1\sigma_{12}$	e(MA_d)	$(\gamma_2/\sigma_2)\sigma_1^2 - 2\gamma_2\sigma_{12}/\sigma_2^2$
e(F)	F from 1 stage	e(R)	OLS R from 1 stage
e(adj_R)	adjusted R from 1 stage	e(chi2)	Probit $\chi^2$ from 1 stage
e(r2_p)	Probit Pseudo R from 1 stage		

If `estimates_hold` is specified, then the above results are also returned along with typical estimation results returned by Stata after estimation. See [P] `estimates`.

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